

DNN Model and Hardware Co-Design

ISCA Tutorial (2019)

Website: <http://eyeriss.mit.edu/tutorial.html>

Approaches

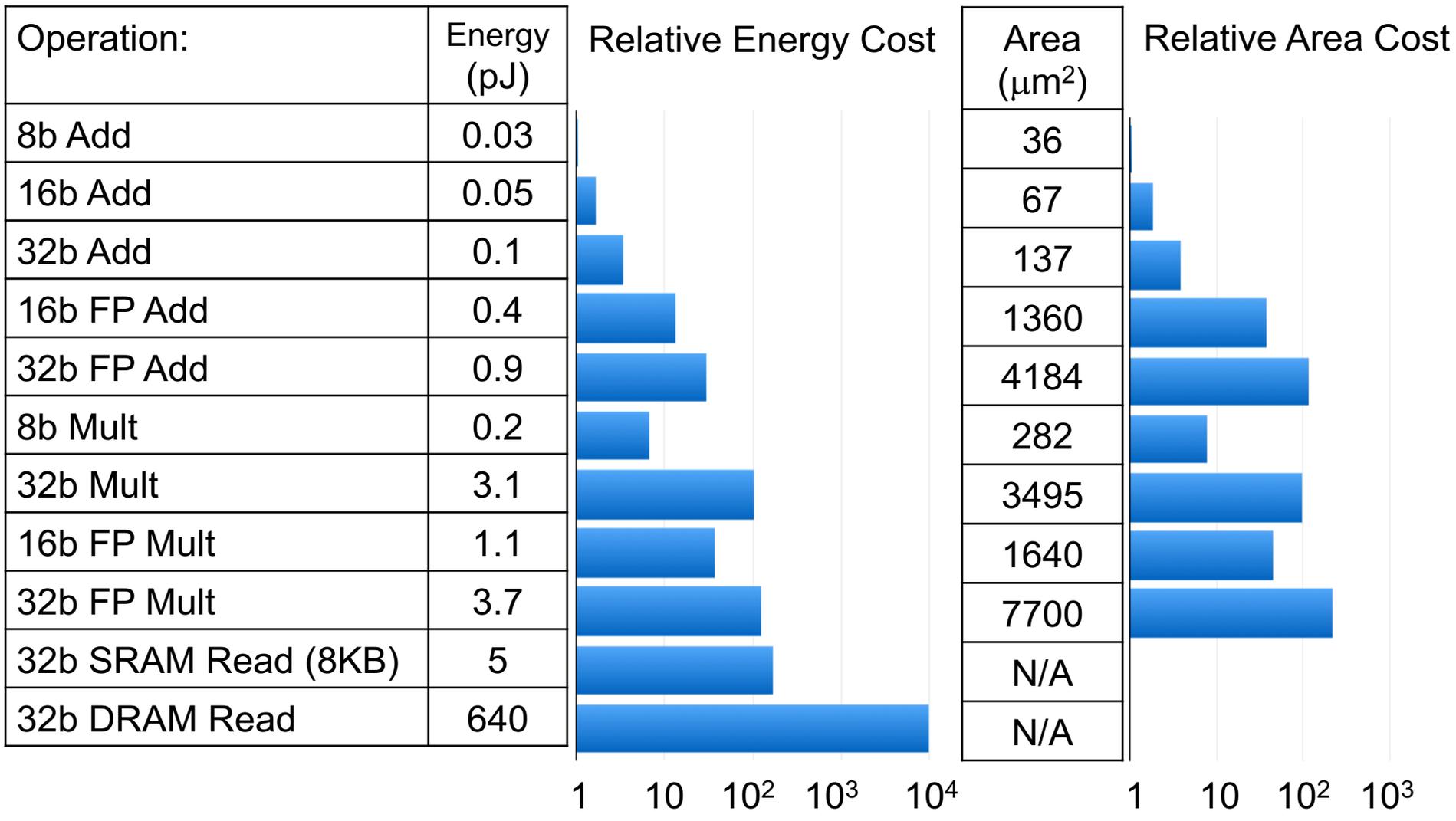
- **Reduce size of operands for storage/compute**
 - Floating point → Fixed point
 - Bit-width reduction
 - Non-linear quantization
- **Reduce number of operations for storage/compute**
 - Exploit Activation Statistics (Compression)
 - Network Pruning
 - Compact Network Architectures

Taxonomy

- **Precision** refers to the **number of levels**
 - Number of bits = \log_2 (number of levels)
- **Quantization**: mapping data to a smaller set of **levels**
 - Linear, e.g., fixed-point
 - Non-linear
 - Computed (e.g., floating point, log-domain)
 - Table lookup (e.g., learned)

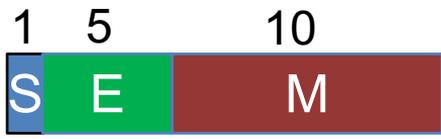
Objective: Reduce size to improve speed and/or reduce energy while preserving accuracy

Cost of Operations



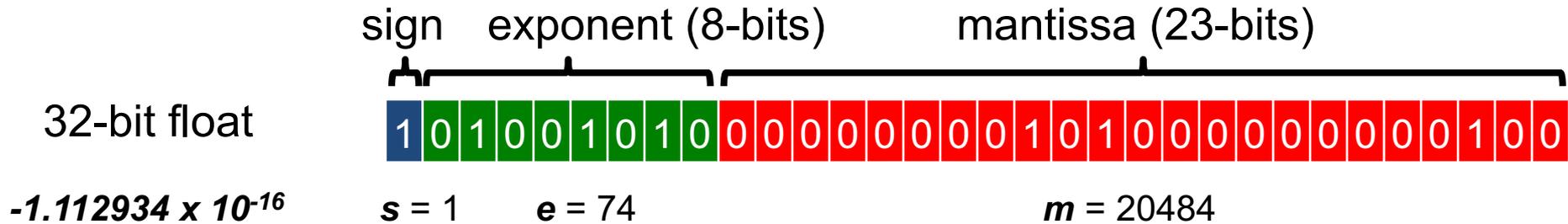
[Horowitz, "Computing's Energy Problem (and what we can do about it)", ISSCC 2014]

Number Representation

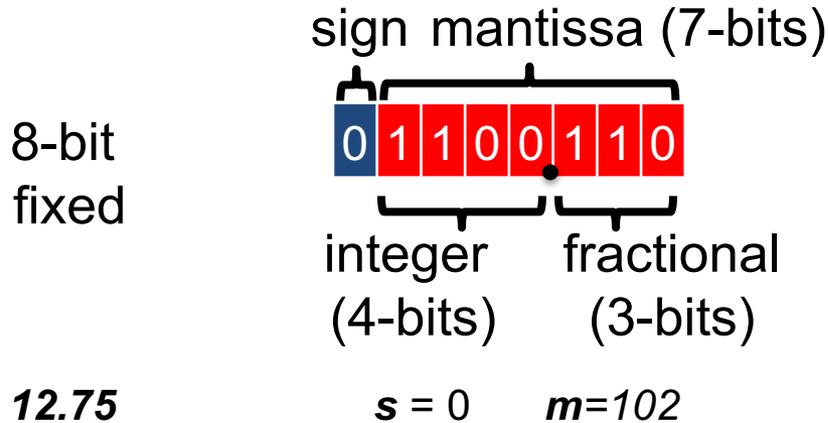
		Range	Accuracy
FP32		$10^{-38} - 10^{38}$.000006%
FP16		$6 \times 10^{-5} - 6 \times 10^4$.05%
Int32		$0 - 2 \times 10^9$	$\frac{1}{2}$
Int16		$0 - 6 \times 10^4$	$\frac{1}{2}$
Int8		$0 - 127$	$\frac{1}{2}$

Floating Point → Fixed Point

Floating Point

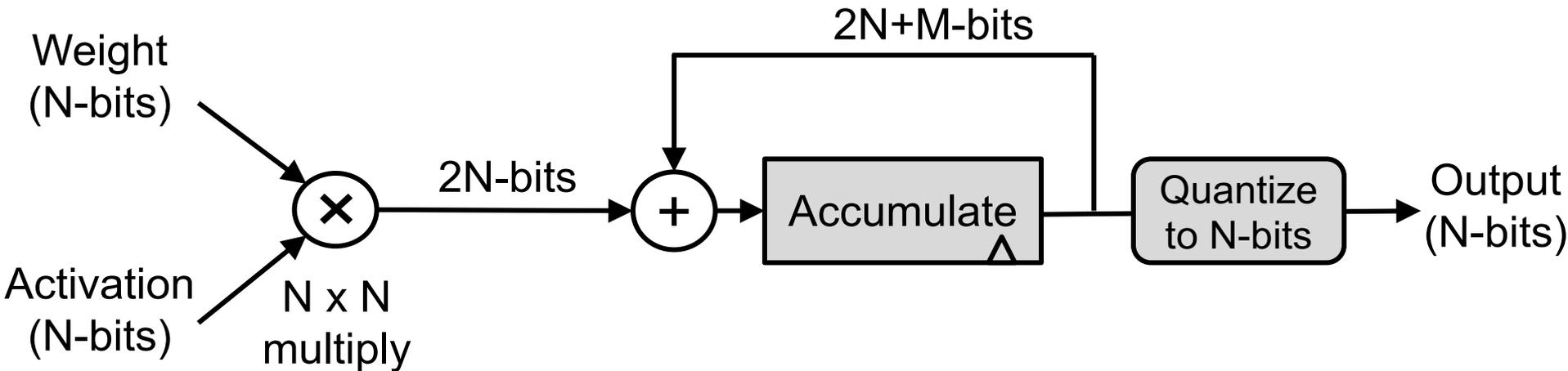


Fixed Point



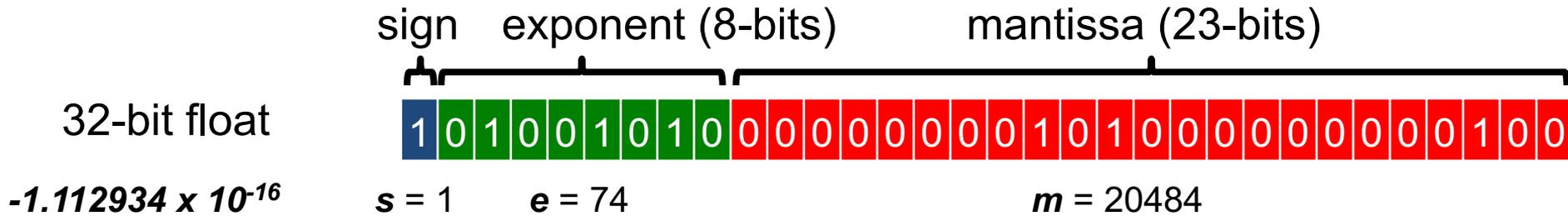
N-bit Precision

For no loss in precision, **M** is determined based on largest filter size (in the range of 10 to 16 bits for popular DNNs)

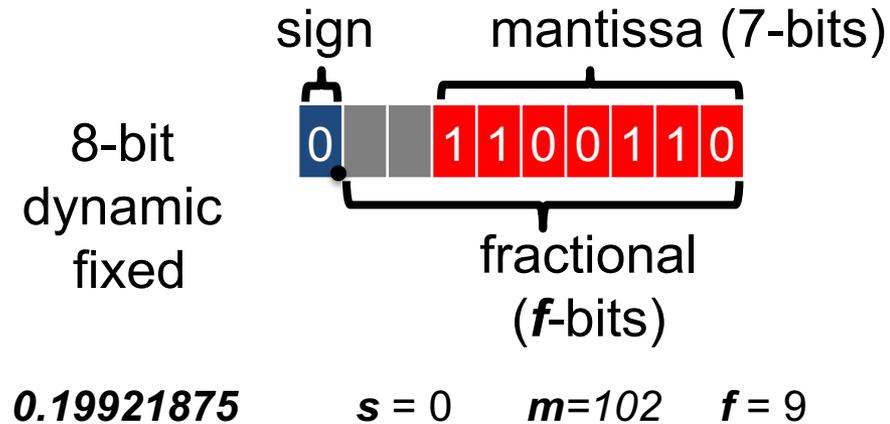
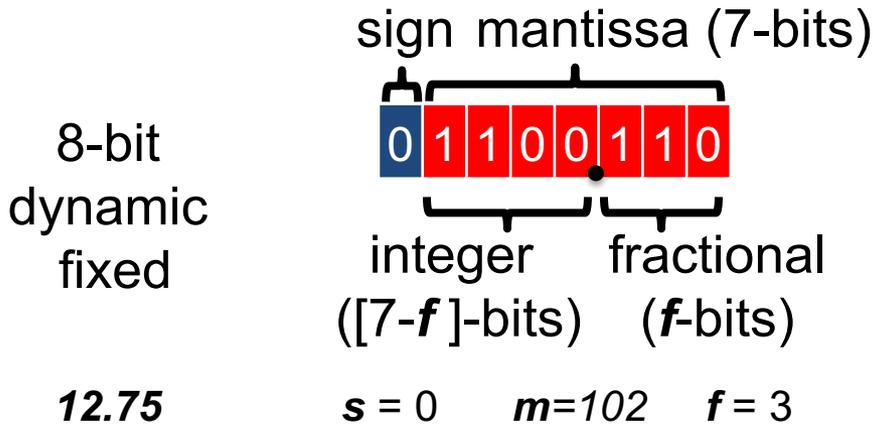


Dynamic Fixed Point

Floating Point



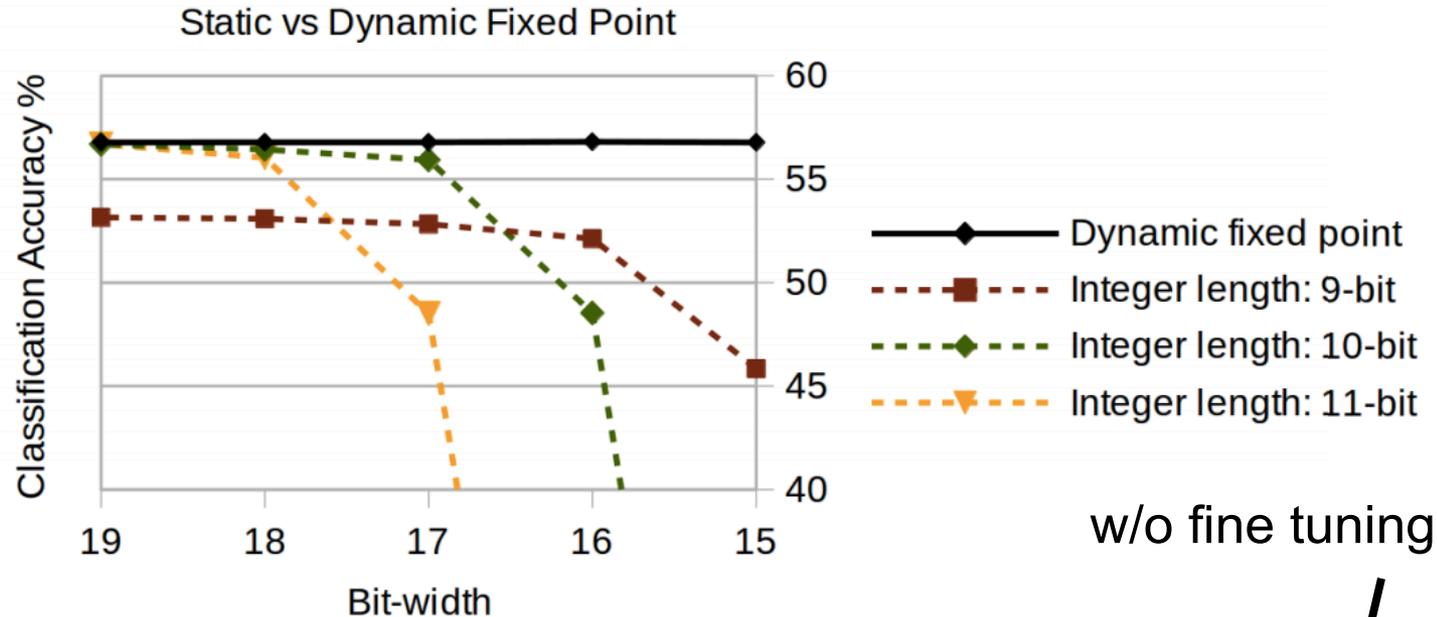
Fixed Point



Allow f to vary based on data type and layer

Impact on Accuracy

Top-1 accuracy
of CaffeNet
on ImageNet



	Layer outputs	CONV parameters	FC parameters	32-bit floating point baseline	Fixed point accuracy
LeNet (Exp 1)	4-bit	4-bit	4-bit	99.1%	99.0% (98.7%)
LeNet (Exp 2)	4-bit	2-bit	2-bit	99.1%	98.8% (98.0%)
Full CIFAR-10	8-bit	8-bit	8-bit	81.7%	81.4% (80.6%)
SqueezeNet top-1	8-bit	8-bit	8-bit	57.7%	57.1% (55.2%)
CaffeNet top-1	8-bit	8-bit	8-bit	56.9%	56.0% (55.8%)
GoogLeNet top-1	8-bit	8-bit	8-bit	68.9%	66.6% (66.1%)

Avoiding Dynamic Fixed Point

Batch normalization 'centers' dynamic range

AlexNet
(Layer 6)

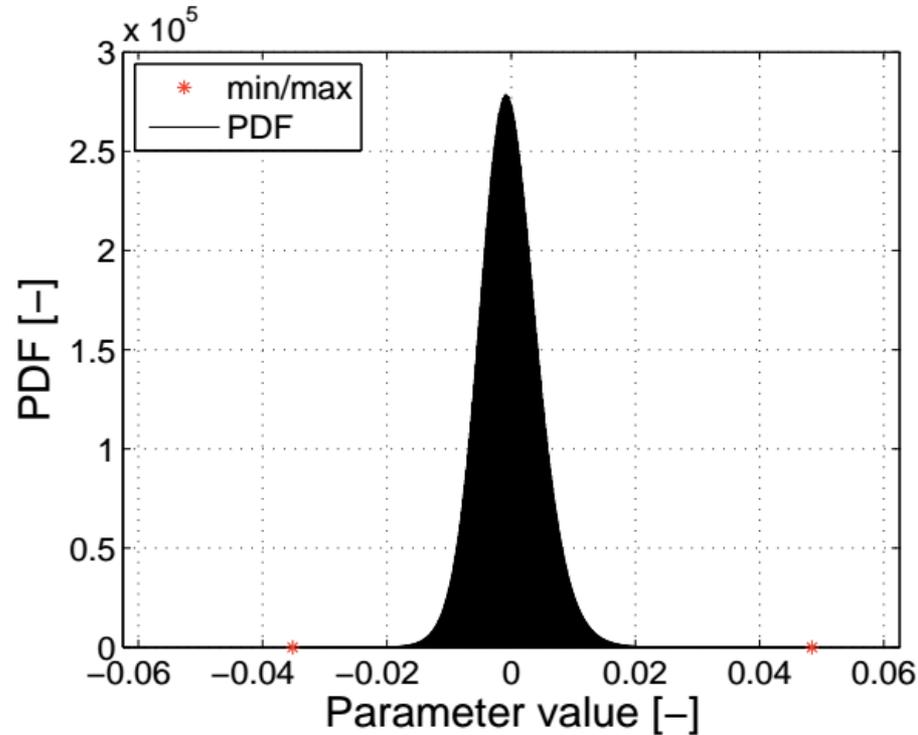


Image Source: Moons
et al, WACV 2016

'Centered' dynamic ranges might reduce need for
dynamic fixed point

Nvidia PASCAL

“New half-precision, **16-bit floating point instructions** deliver over **21 TeraFLOPS** for unprecedented training performance. **With 47 TOPS (tera-operations per second) of performance, new 8-bit integer instructions** in Pascal allow AI algorithms to deliver real-time responsiveness for deep learning inference.”

– Nvidia.com (April 2016)



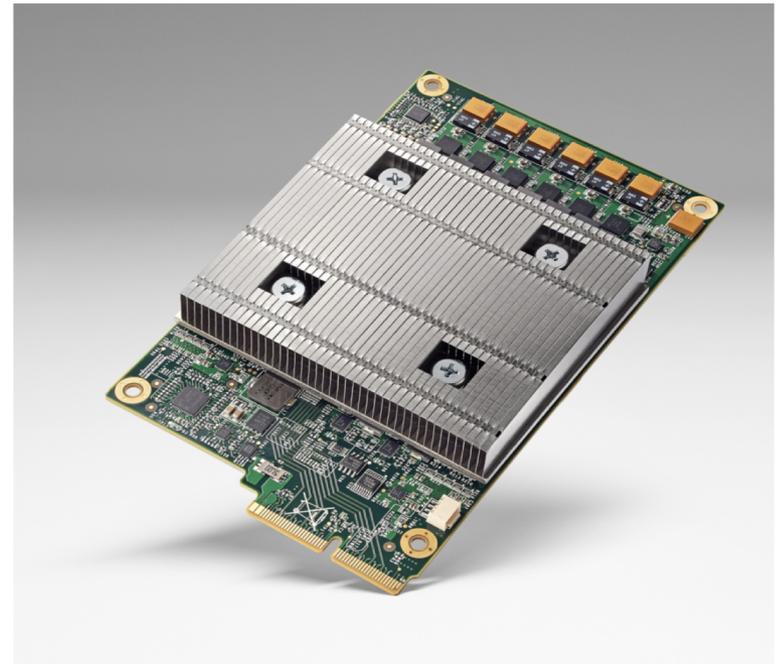
Google's Tensor Processing Unit (TPU)

“ With its TPU Google has seemingly focused on delivering the data really quickly by **cutting down on precision**. Specifically, it doesn't rely **on floating point precision like a GPU**

....

Instead the chip uses integer math...TPU used **8-bit integer**.”

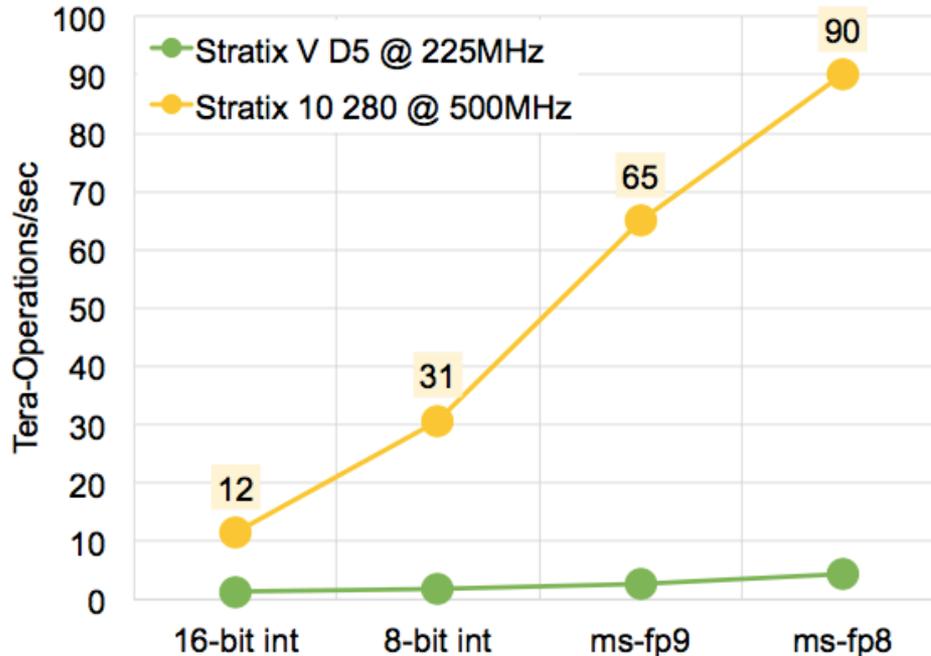
- Next Platform (May 19, 2016)



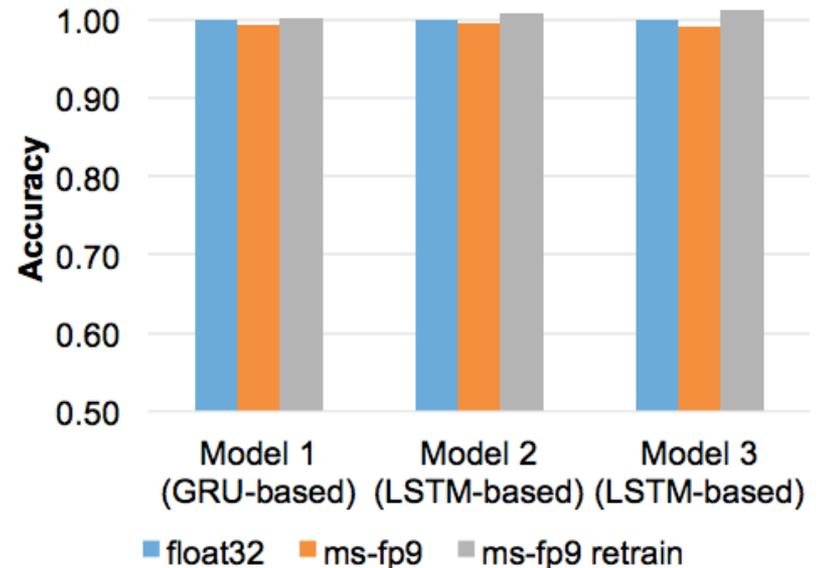
Microsoft BrainWave

Narrow Precision for Inference

FPGA Performance vs. Data Type



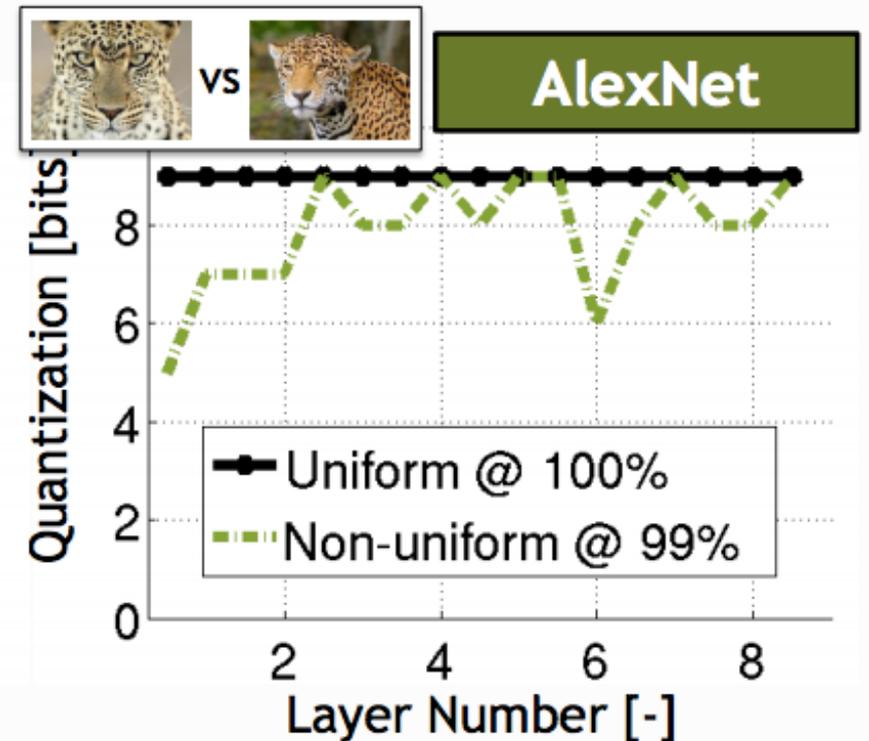
Impact of Narrow Precision on Accuracy



Custom 8-bit floating point format (“ms-fp8”)

Precision Varies from Layer to Layer

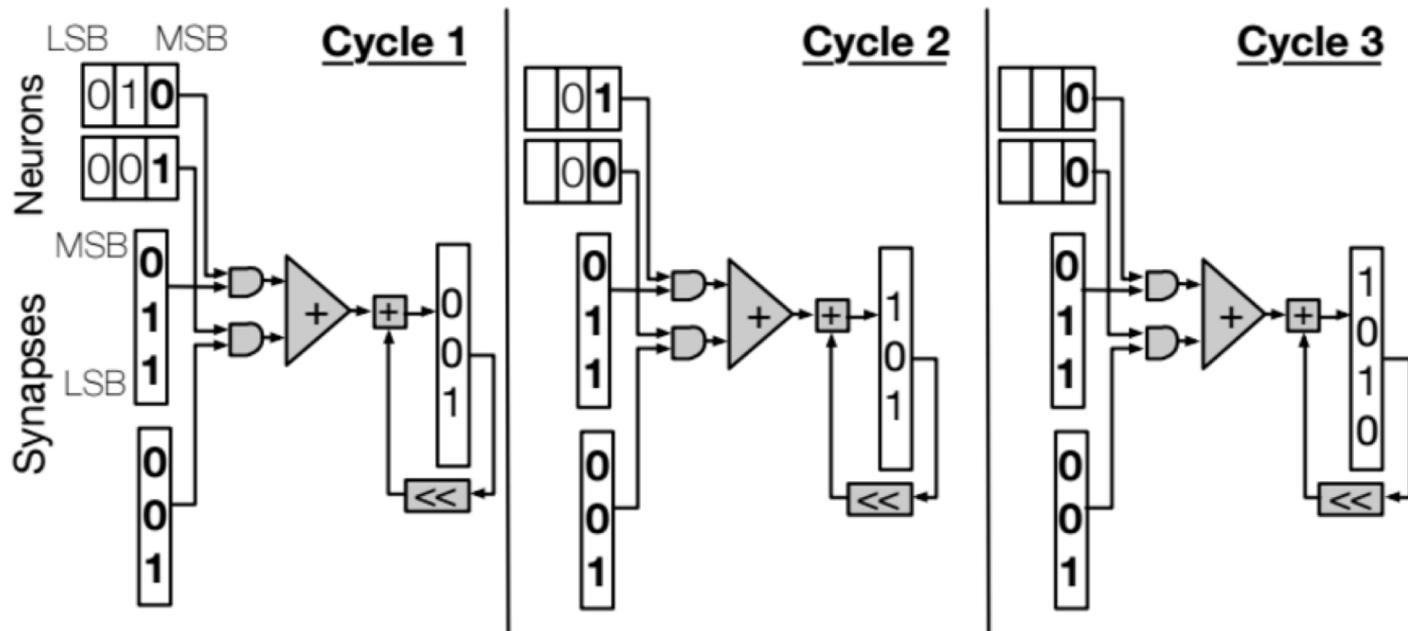
Tolerance	Bits per layer (I+F)
AlexNet (F=0)	
1%	10-8-8-8-8-8-6-4
2%	10-8-8-8-8-8-5-4
5%	10-8-8-8-7-7-5-3
10%	9-8-8-8-7-7-5-3



Bitwidth Scaling (Speed)

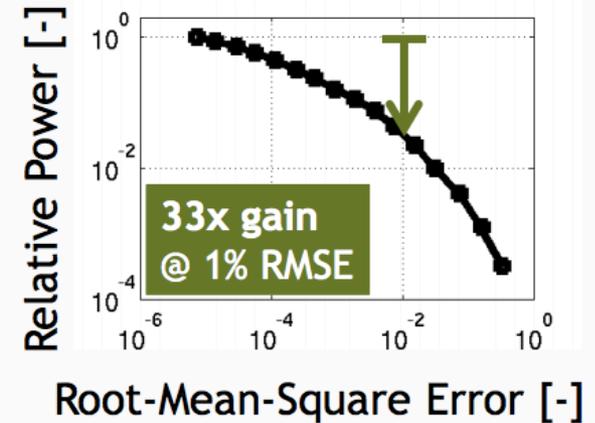
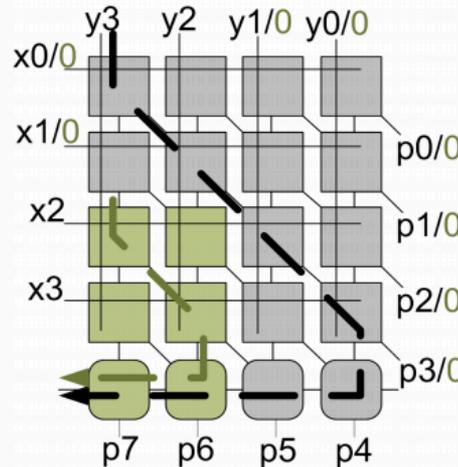
Bit-Serial Processing: Reduce Bit-width → Skip Cycles
Speed up of 2.24x vs. 16-bit fixed

$$\sum_{i=0}^{N_i-1} s_i \times n_i = \sum_{i=0}^{N_i-1} s_i \times \sum_{b=0}^{P-1} n_i^b \times 2^b = \sum_{b=0}^{P-1} 2^b \times \sum_{i=0}^{N_i-1} n_i^b \times S_i$$



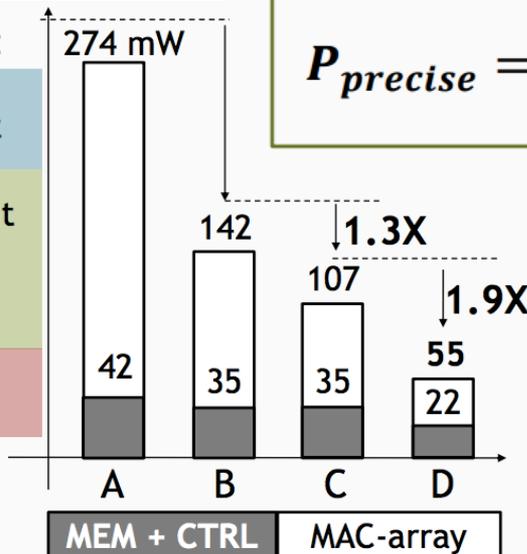
Bitwidth Scaling (Power)

Reduce Bit-width →
Shorter Critical Path
→ Reduce Voltage



AlexNet Layer 2 example:

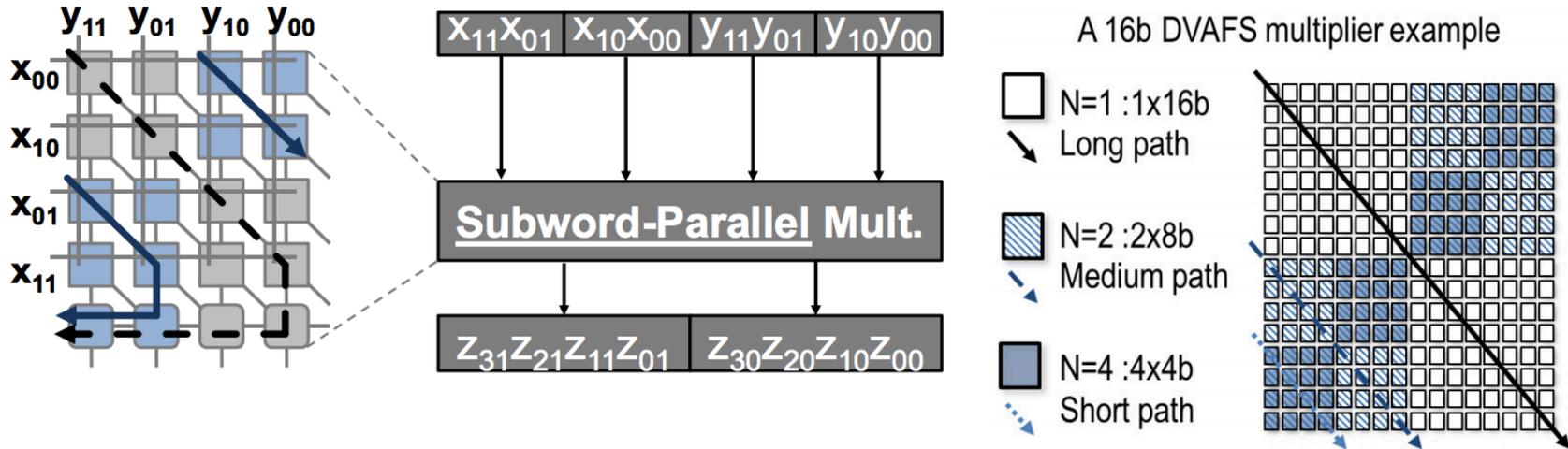
- A. 2D-baseline @ 16 bit
- B. Precision-Scaling @ 7-7 bit
- C. Voltage-Scaling @ 0.9 V
- D. Sparse operation guarding



$$P_{precise} = \alpha C f V^2 \Rightarrow P_{imprecise} = \frac{\alpha}{k_1} C f \left(\frac{V}{k_2}\right)^2$$

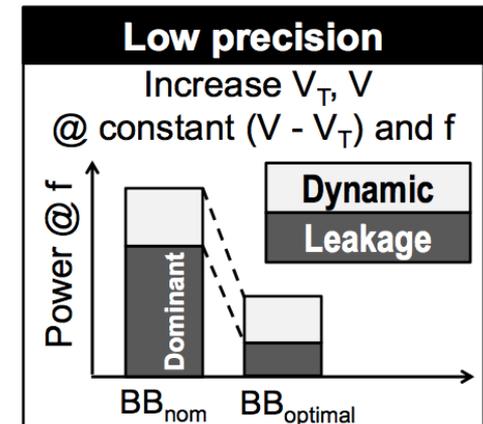
**Power reduction of
2.56x vs. 16-bit fixed
On AlexNet Layer 2**

Reconfigure Spatial Multiply



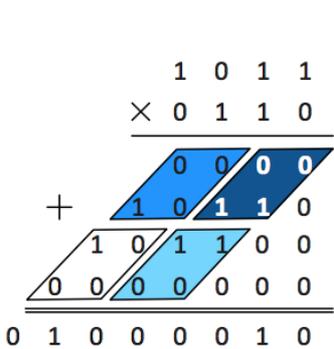
$$E_{\text{precise}} \sim \alpha C f V^2 \quad \text{constant throughput} \Rightarrow E_{\text{imprecise}} \sim \frac{\alpha}{k_3} C \frac{f}{N} \left(\frac{V}{k_4}\right)^2$$

Configure 16b x 16b multiplication into two 8x8b or four 4x4b (up to 256-64=192 adders are idle).
Body bias to reduce leakage at low precision since more adders are idle (1.2x reduction)

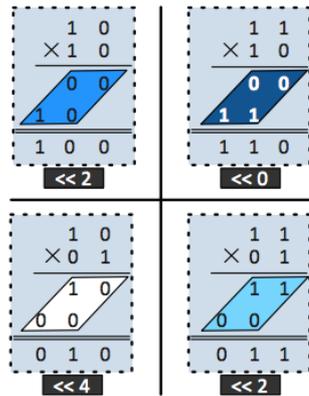


Reconfigure Spatial Multiply

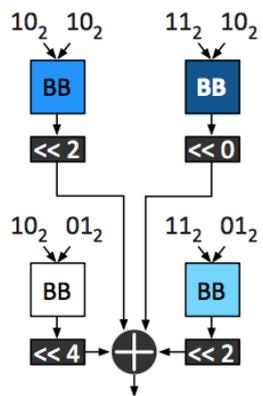
Build larger multipliers (Fused Unit) from small 2x2 multipliers with programmable shifters (BitBrick)



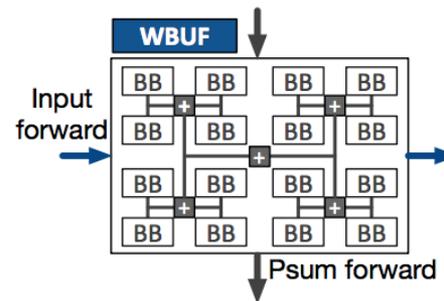
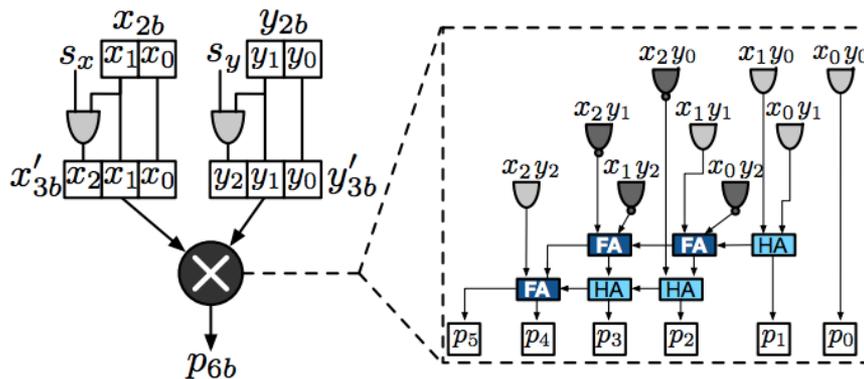
(a) A 4-bit multiplication ($6_{10} \times 11_{10} = 66_{10}$)



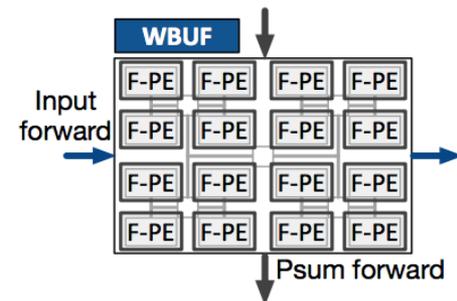
(b) Decomposing the 4-bit multiplication to four 2-bit multiplications.



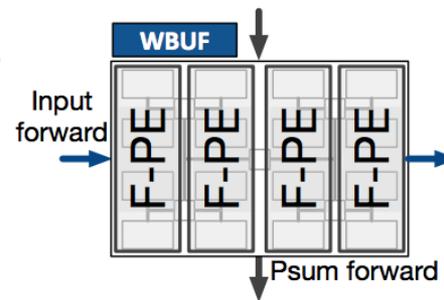
(c) Mapping decomposed multiplications to BitBricks (BBs).



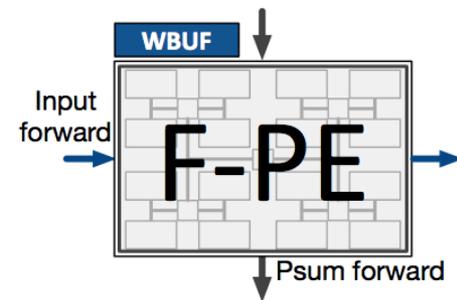
(a) Fusion Unit with 16 BitBricks



(b) 16x Parallelism, Binary (1-bit) or Ternary (2-bit)



(c) 4x Parallelism, Mixed-Bitwidth (2-bit weights, 8-bit inputs)



(d) No Parallelism, 8-bits

One 8bx8b, four 2bx8b, sixteen 2bx2b

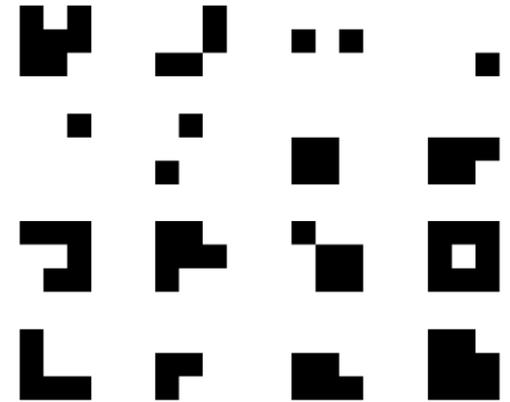
Binary Nets

- **Binary Connect (BC)**

- Weights $\{-1, 1\}$, Activations 32-bit float
- MAC \rightarrow addition/subtraction
- Accuracy loss: **19%** on AlexNet

[Courbariaux, NeurIPS 2015]

Binary Filters



- **Binarized Neural Networks (BNN)**

- Weights $\{-1, 1\}$, Activations $\{-1, 1\}$
- MAC \rightarrow XNOR
- Accuracy loss: **29.8%** on AlexNet

[Courbariaux, arXiv 2016]

Scale the Weights and Activations

- **Binary Weight Nets (BWN)**

- Weights $\{-\alpha, \alpha\}$ → except first and last layers are 32-bit float
- Activations: 32-bit float
- α determined by the l_1 -norm of all weights in a filter
- Accuracy loss: **0.8%** on AlexNet

- **XNOR-Net**

- Weights $\{-\alpha, \alpha\}$
- Activations $\{-\beta_i, \beta_i\}$ → except first and last layers are 32-bit float
- β_i determined by the l_1 -norm of all activations across channels **for given position i** of the input feature map
- Accuracy loss: **11%** on AlexNet

Hardware needs to support both activation precisions

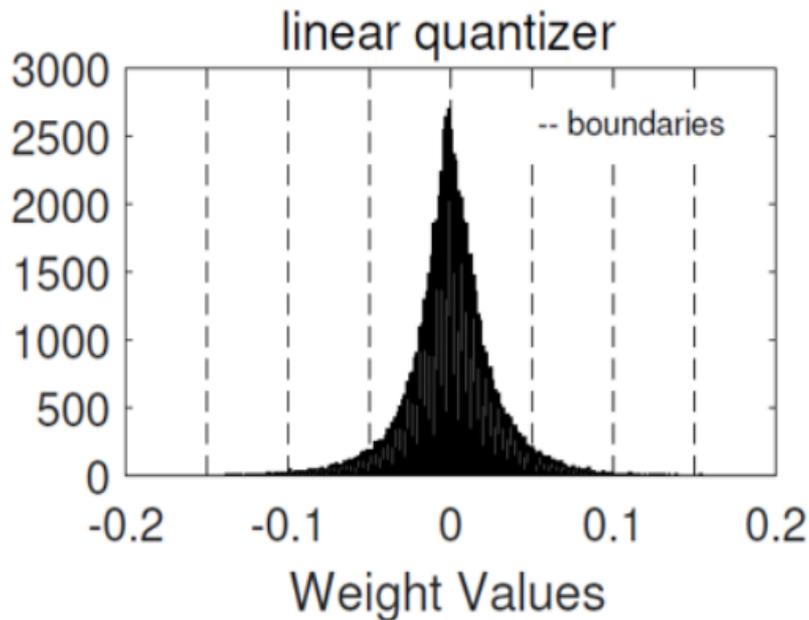
Scale factors (α, β_i) can change per filter or position in filter

Ternary Nets

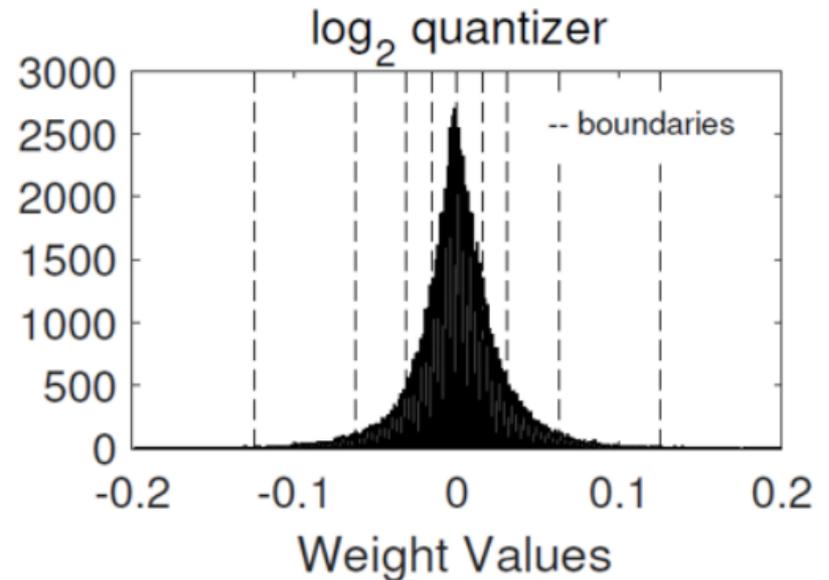
- **Allow for weights to be zero**
 - Increase sparsity, but also increase number of bits (2-bits)
- **Ternary Weight Nets (TWN)** [Li et al., arXiv 2016]
 - Weights $\{-w, 0, w\}$ \rightarrow except first and last layers are 32-bit float
 - Activations: 32-bit float
 - Accuracy loss: **3.7%** on AlexNet
- **Trained Ternary Quantization (TTQ)** [Zhu et al., ICLR 2017]
 - Weights $\{-w_1, 0, w_2\}$ \rightarrow except first and last layers are 32-bit float
 - Activations: 32-bit float
 - Accuracy loss: **0.6%** on AlexNet

Computed Non-linear Quantization

Log Domain Quantization



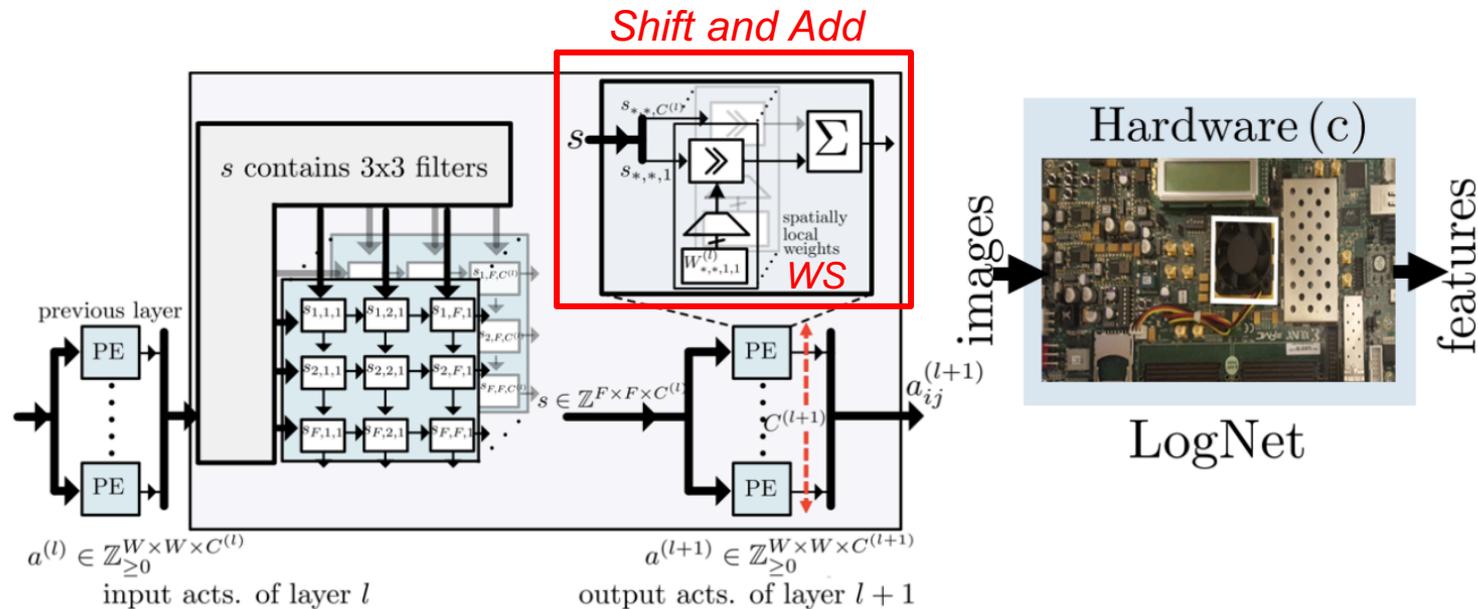
$$\text{Product} = X * W$$



$$\text{Product} = X \ll W$$

Log Domain Quantization

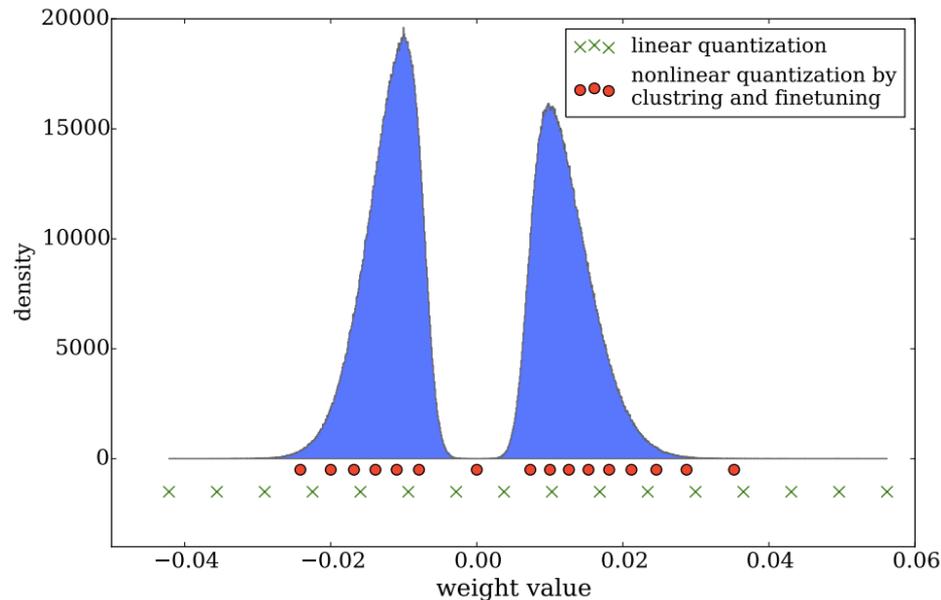
- **Weights: 5-bits for CONV, 4-bit for FC; Activations: 4-bits**
- Accuracy loss: **3.2%** on AlexNet



[Miyashita et al., arXiv 2016],
 [Lee et al., LogNet, ICASSP 2017]

Reduce Precision Overview

- **Learned mapping of data to quantization levels (e.g., k-means)**



*Implement with
look up table*

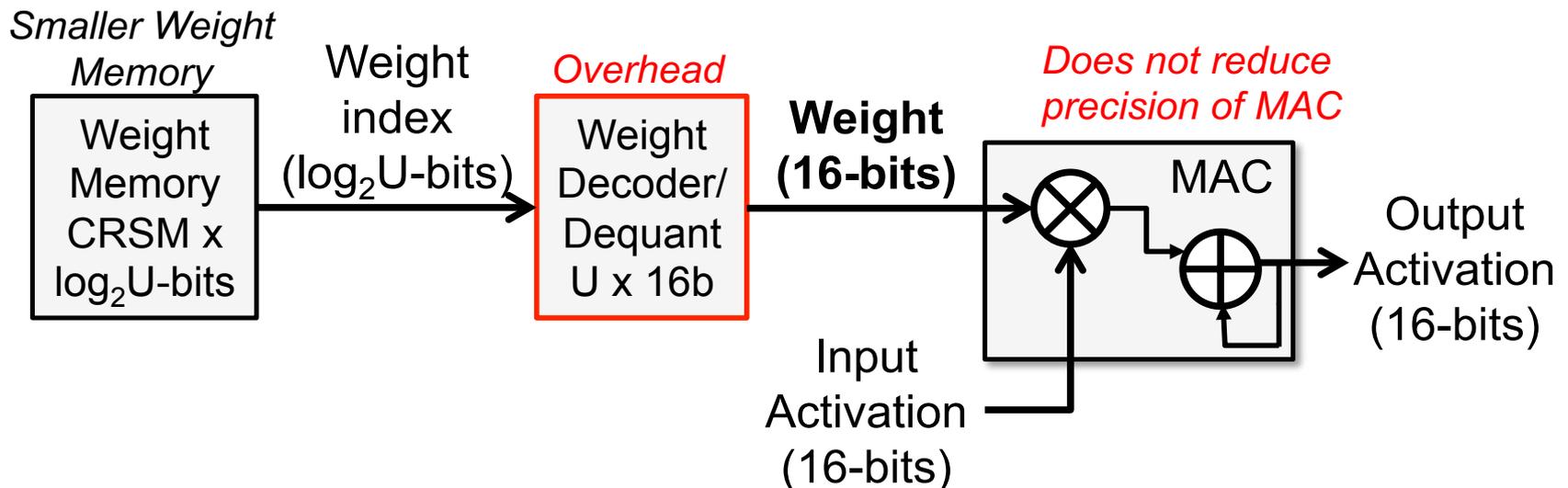
[Han et al., ICLR 2016]

- **Additional Properties**
 - **Fixed or Variable (across data types, layers, channels, etc.)**

Non-Linear Quantization Table Lookup

Trained Quantization: Find K weights via K -means clustering to reduce number of unique weights *per layer* (weight sharing)

Example: AlexNet (no accuracy loss)
256 unique weights for CONV layer
16 unique weights for FC layer



Consequences: Narrow weight memory and second access from (small) table

Summary of Reduce Precision

Category	Method	Weights (# of bits)	Activations (# of bits)	Accuracy Loss vs. 32-bit float (%)
Dynamic Fixed Point	w/o fine-tuning	8	10	0.4
	w/ fine-tuning	8	8	0.6
Reduce weight	Ternary weights Networks (TWN)	2*	32	3.7
	Trained Ternary Quantization (TTQ)	2*	32	0.6
	Binary Connect (BC)	1	32	19.2
	Binary Weight Net (BWN)	1*	32	0.8
Reduce weight and activation	Binarized Neural Net (BNN)	1	1	29.8
	XNOR-Net	1*	1	11
Non-Linear	LogNet	5(conv), 4(fc)	4	3.2
	Weight Sharing	8(conv), 4(fc)	16	0

* first and last layers are 32-bit float